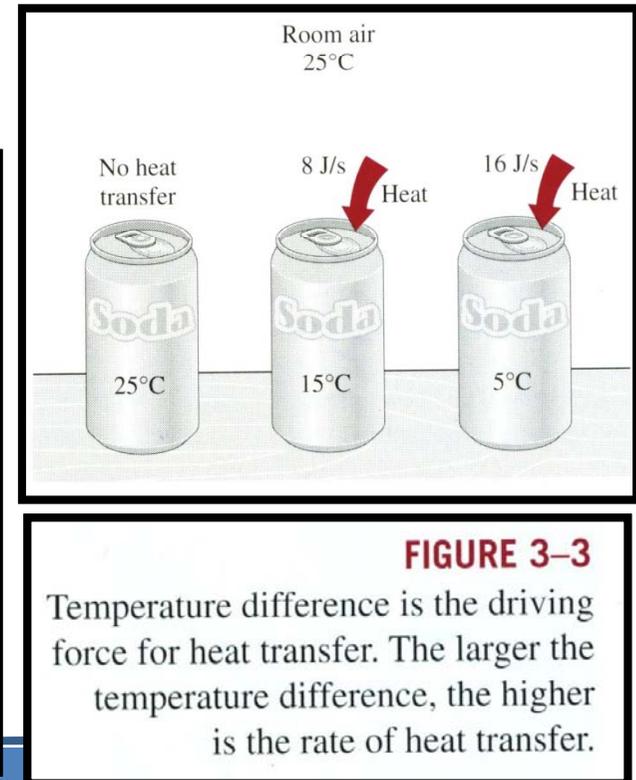
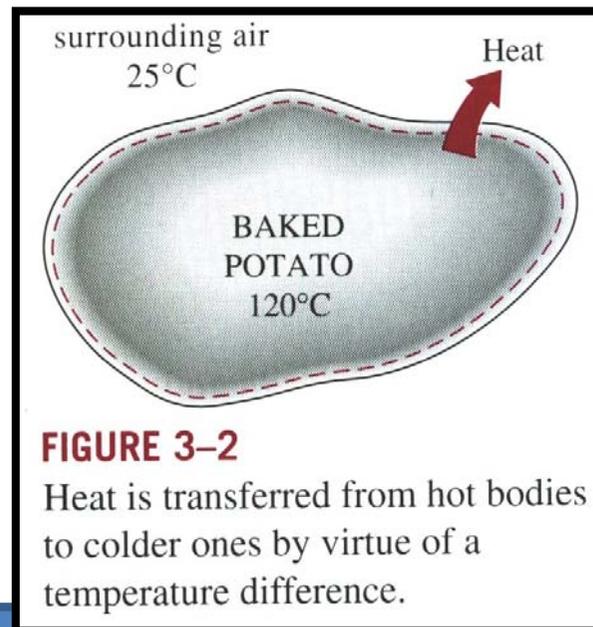
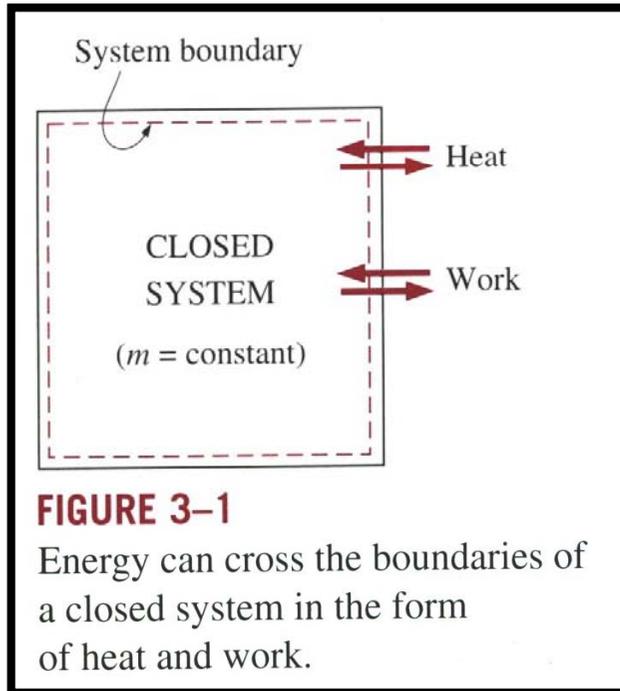
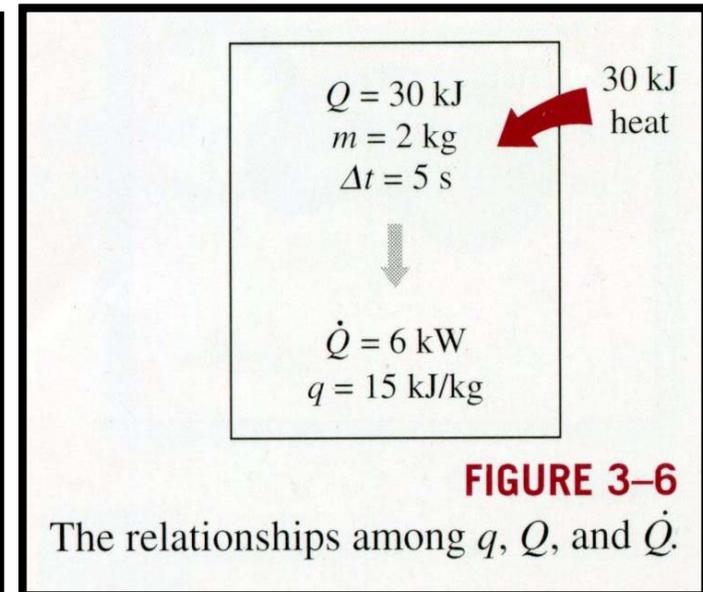
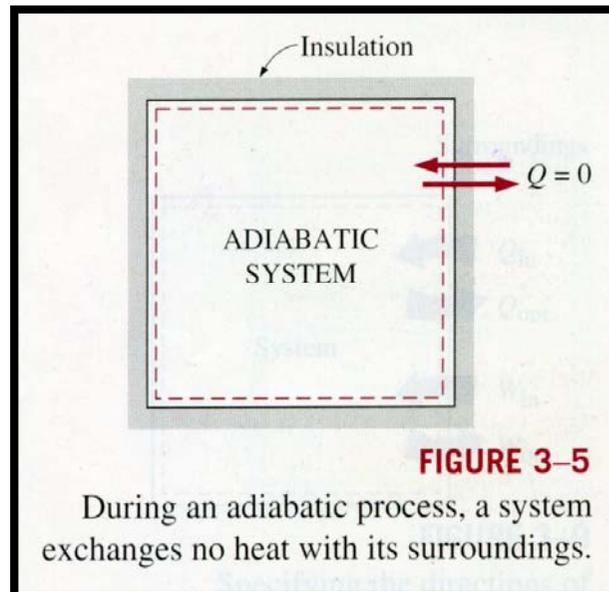
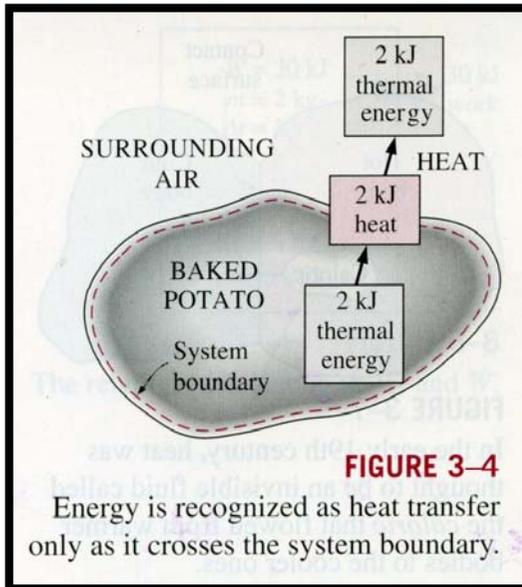


# 3-1. HEAT TRANSFER



# 3-1. HEAT TRANSFER



## 3-1. HEAT TRANSFER

Heat Transfer per unit mass

$$q = \frac{Q}{m} \quad (\text{kJ/kg})$$

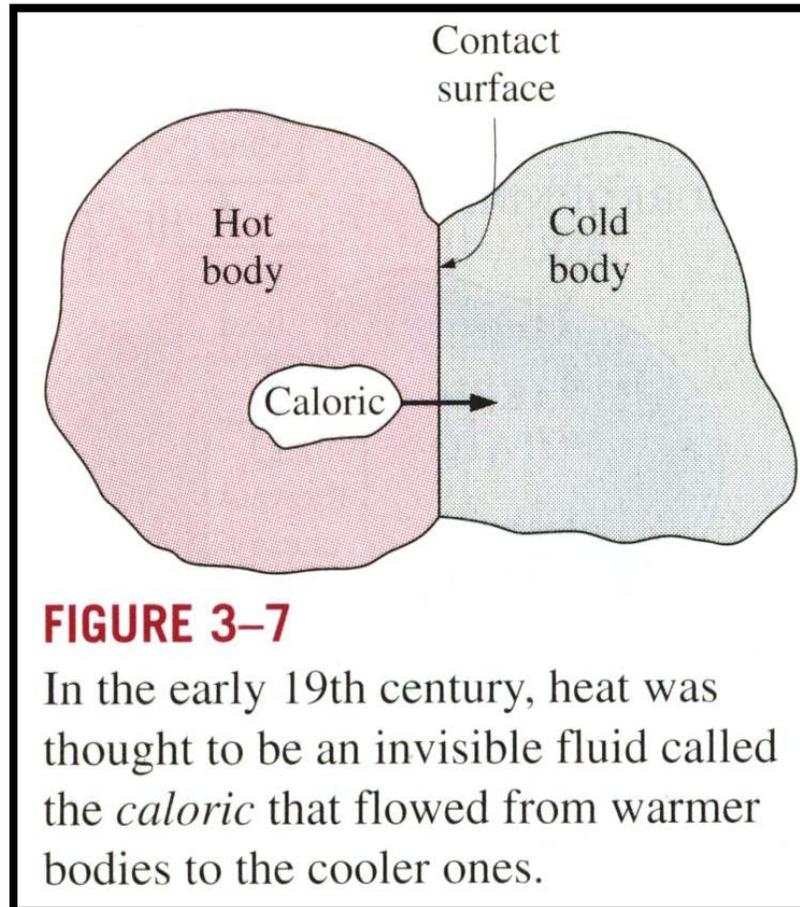
Heat Transfer rate is denoted  $\dot{Q}$

$$Q = \int_{t_1}^{t_2} \dot{Q} dt \quad (\text{kJ})$$

Heat Transfer rate is denoted  $\dot{Q}$

$$Q = \dot{Q} \Delta t \quad (\text{kJ})$$
$$\Delta t = t_2 - t_1$$

# Historical Background on Heat



## Energy transfer by Work

Work done per unit mass of system,  $w$

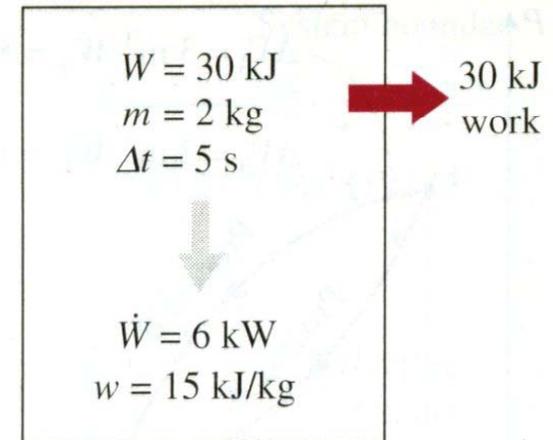
$$w = \frac{W}{m} \quad (\text{kJ/kg})$$

Work done per unit time is called *power*

$$\dot{W} \quad \text{kJ/s, or kW}$$

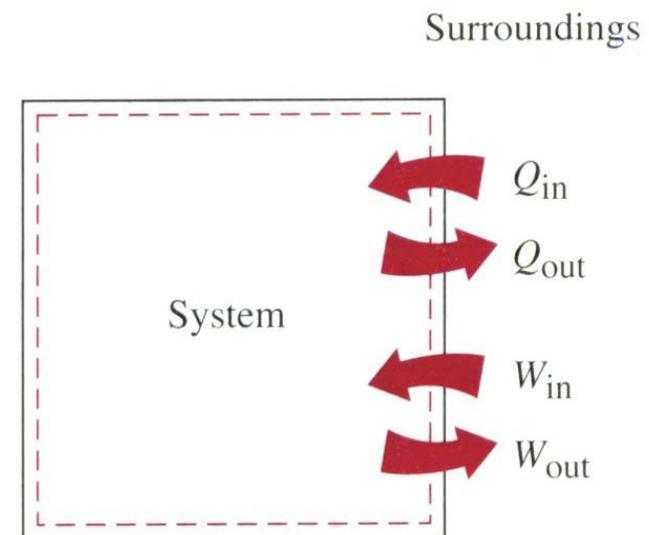
Path function have inexact differential designated by the symbol  $\delta$

Exact differential designated by the symbol  $d$



**FIGURE 3–8**

The relationships among  $w$ ,  $W$ , and  $\dot{W}$ .



**FIGURE 3–9**

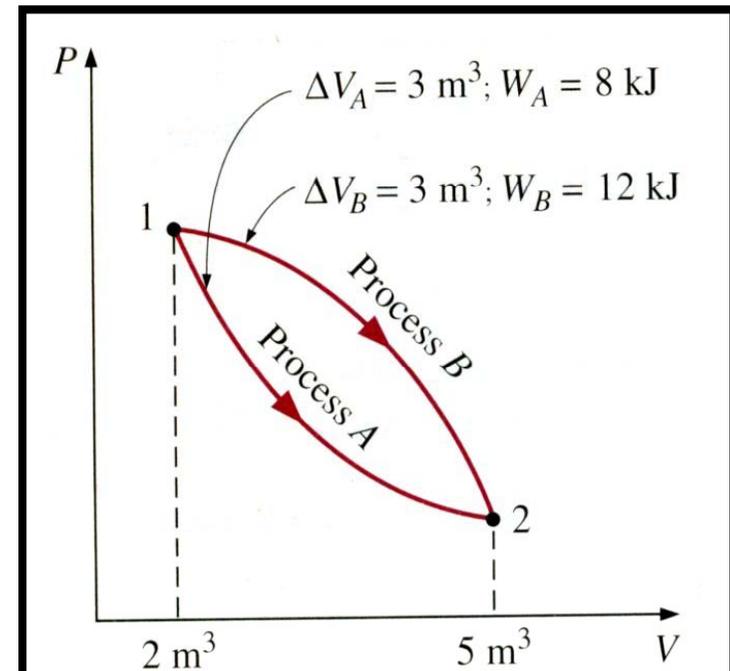
Specifying the directions of heat and work.

The volume change during a process between states 1 and 2 is

$$\int_1^2 dV = V_2 - V_1 = \Delta V$$

Total work done during process 1-2

$$\int_1^2 \delta W = W_{12} \quad (\text{not } \Delta W)$$



**FIGURE 3-10**

Properties are point functions; but heat and work are path functions (their magnitudes depend on the path followed).

# Electrical Work

$$W_e = VN$$

**N** คือปริมาณไฟฟ้าที่ผ่านจุดหนึ่งๆ โดยมีกระแส **1** แอมป์  
แรงเคลื่อน **1** โวลต์ใน **1** นาที

$$\dot{W}_e = VI \quad (\text{W})$$

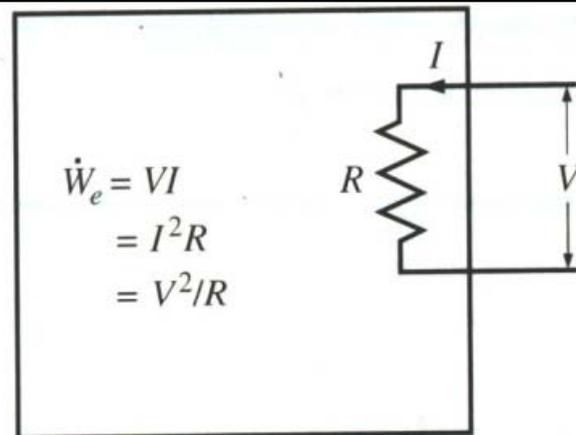
$\dot{W}_e$  is the electrical power

โดยทั่วไปแรงเคลื่อน และกระแสไฟฟ้าแปรผันตามเวลา

$$W_e = \int_1^2 VI \, dt \quad (\text{kJ})$$

**V** และ **I** คงที่

$$W_e = VI \, \Delta t \quad (\text{kJ})$$



**FIGURE 3-15**

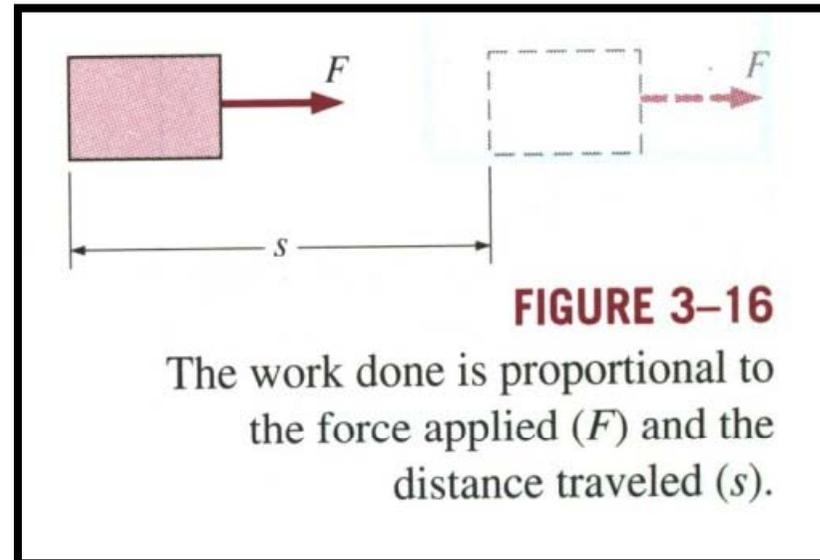
Electrical power in terms of resistance  $R$ , current  $I$ , and potential difference  $V$ .

# MECHANICAL FORMS OF WORK

$$W = Fs \quad (kJ)$$

**F is not constant**

$$W = \int_1^2 F ds \quad (kJ)$$



# Moving Boundary Work

งานที่ได้จากการเคลื่อนที่ของขอบเขต

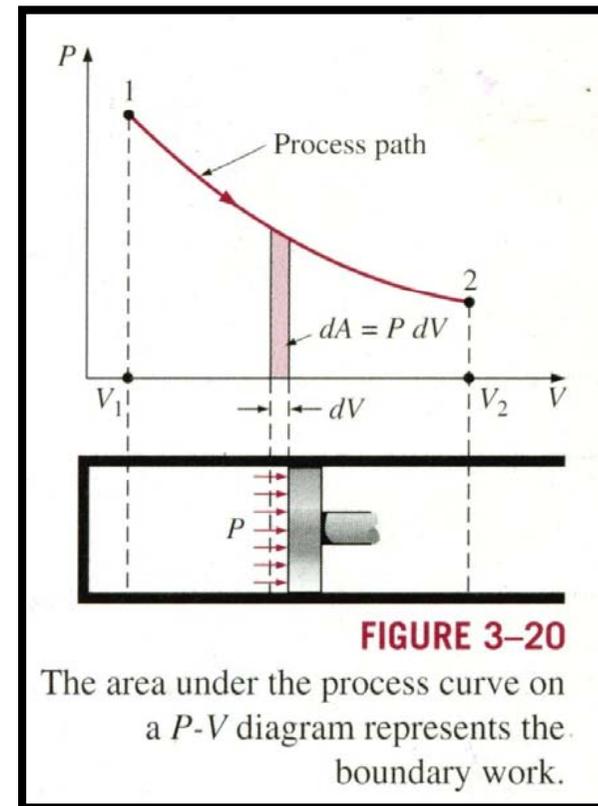
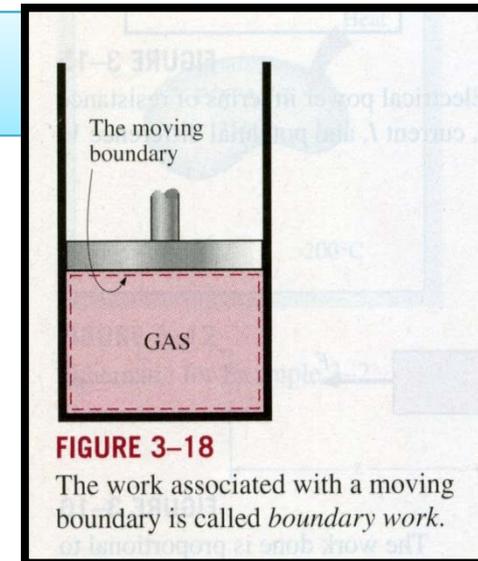
F is not constant

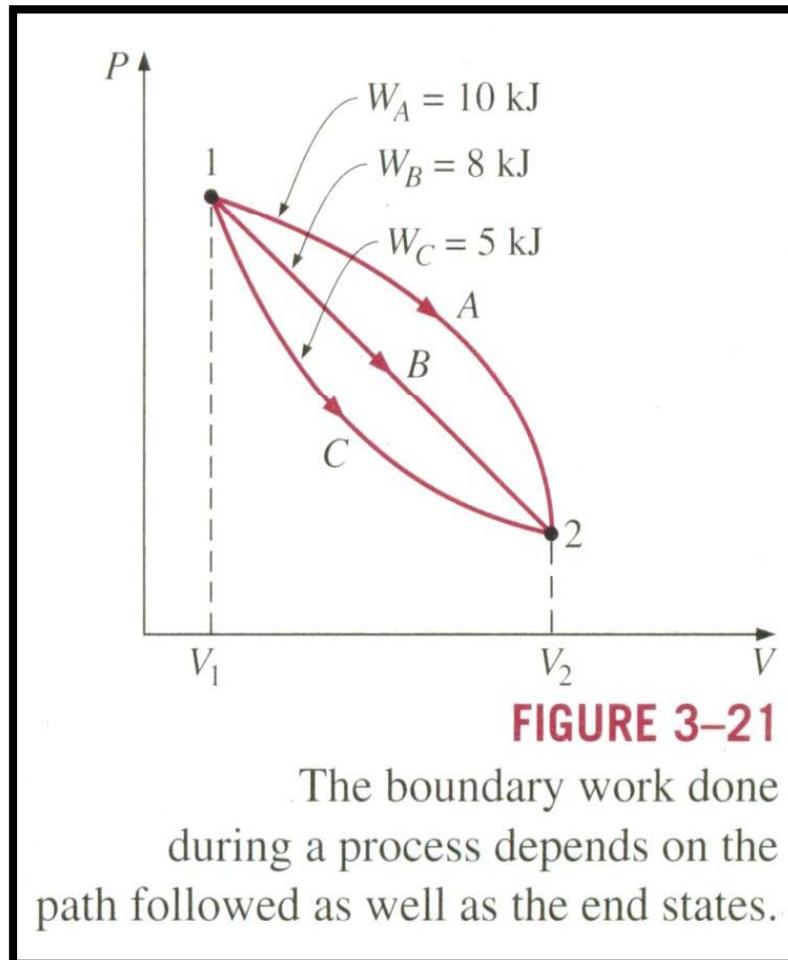
$$\delta W_b = F ds = P A ds = P dV$$

$$W_b = \int_1^2 P dV \quad (\text{kJ})$$

The total area A under the process curve 1-2 is obtained by adding these differential area

$$A_{\text{era}} = A = \int_1^2 dA = \int_1^2 P dV \quad (\text{kJ})$$





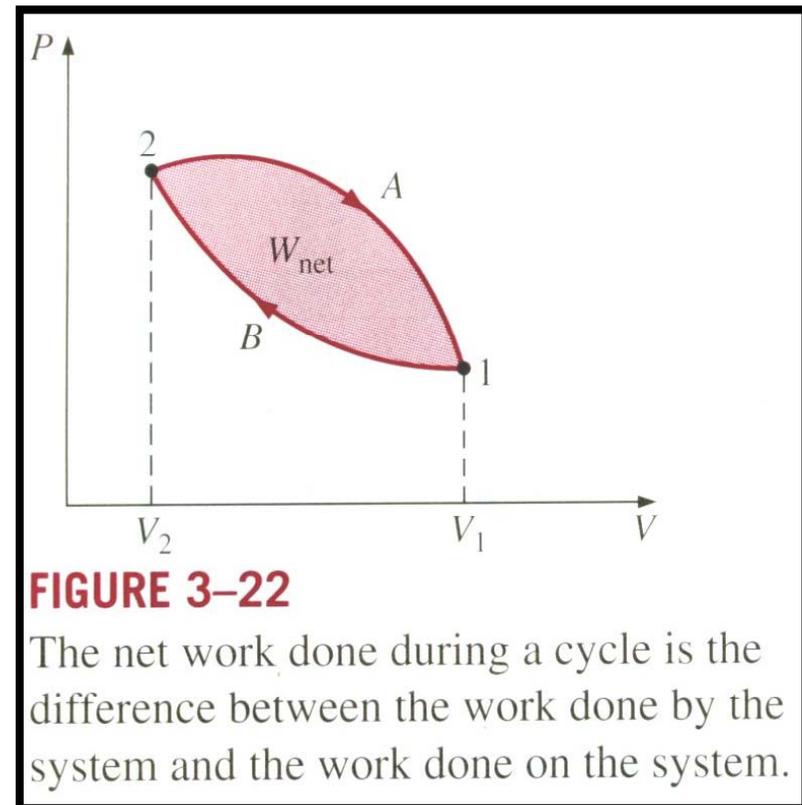
# Moving Boundary Work

$$W_b = \int_1^2 P_i dV \quad (\text{kJ})$$

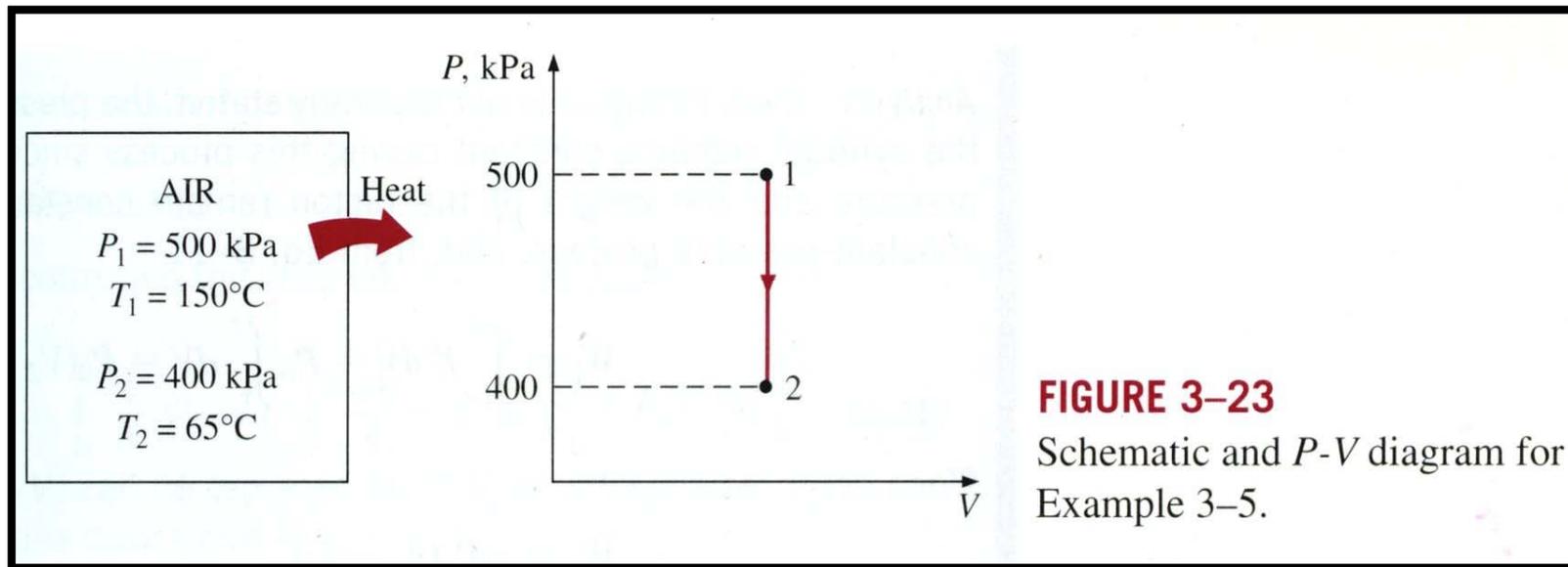
$P_i$  = Pressure is inner face of the piston  
 $W_b$  = represent the amount of energy transferred from the system during an expansion process

$$W_b = W_{friction} + W_{atm} + W_{crank}$$

$$= \int_1^2 (F_{friction} + P_{atm} A + F_{crank}) dx$$



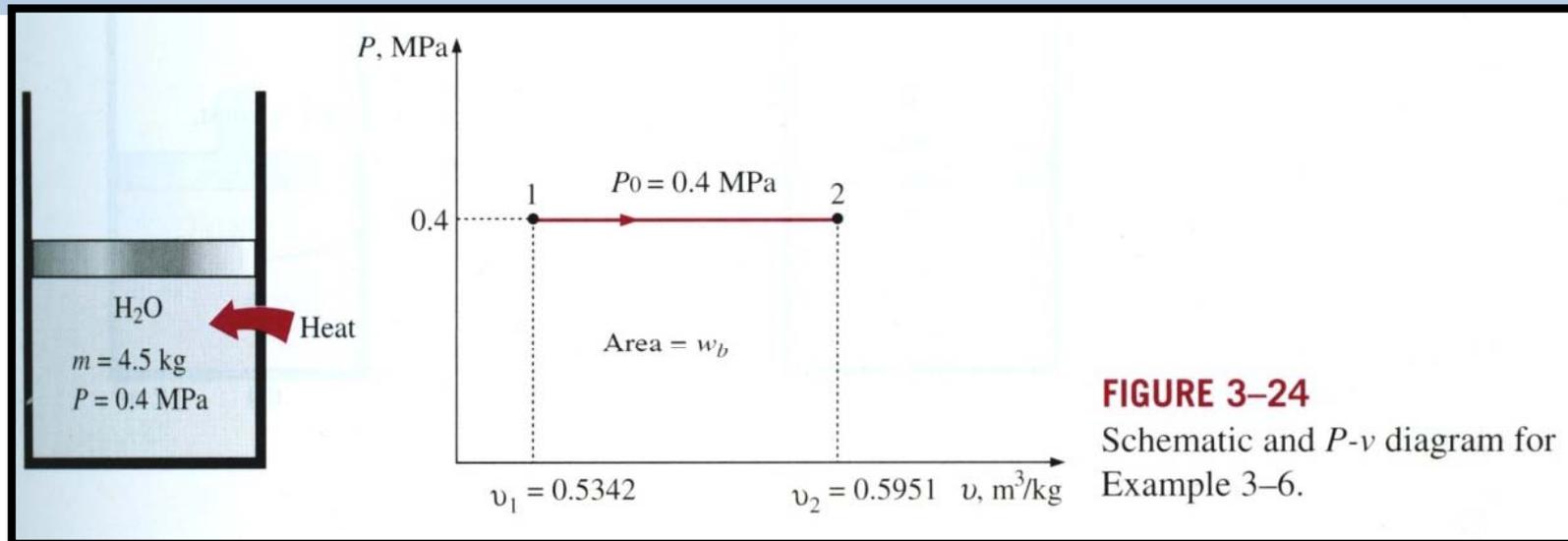
**EXAMPLE 3-5** A rigid tank contains air at 500 kPa and 150 °C . As a result of heat transfer to the surroundings, the temperature and pressure inside the tank drop to 65 °C and 400 kPa, respectively. Determine the boundary work done during this process.



**Analysis:** The boundary work can be determined from eq. 3-11 to be

$$W_b = \int_1^2 P dV = 0 \quad (\text{kJ}), (dv = 0)$$

**EXAMPLE 3-6** A frictionless piston-cylinder device contains 4.5 kg of water vapor at 0.4 MPa and 200 °C. Heat is now transferred to the steam until the temperature reaches 250 °C. If the piston is not attached to the shaft and its mass is constant, determine the work done by the steam during this process.

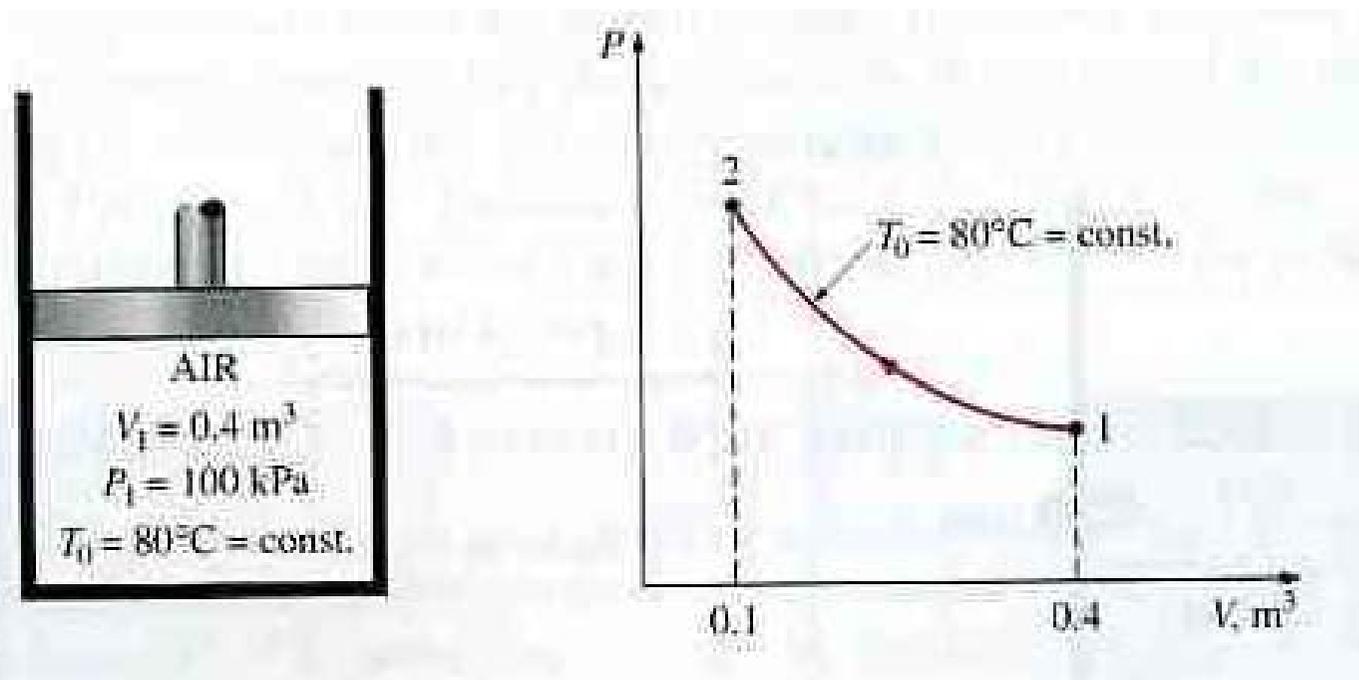


$$W_b = \int_1^2 P_i dV = P_o \int_1^2 dV = P_o (V_2 - V_1) \quad \text{or} \quad W_b = m P_o (V_2 - V_1)$$

$$W_b = (4.5 \text{ kg})(400 \text{ kPa})[(0.5951 - 0.5342) \text{ m}^3 / \text{kg}] = 109.62 \text{ kJ}$$

### EXAMPLE 3-6: Isothermal Compression of an ideal gas

A piston-cylinder device initially contains  $0.4 \text{ m}^3$  of air at  $100 \text{ kPa}$  and  $80^\circ\text{C}$ . The air is now compressed to  $0.1 \text{ m}^3$  in such a way that the temperature inside the cylinder remains constant. Determine the work done during this process.



**FIGURE 3-25**  
Schematic and  $P$ - $V$  diagram  
for Example 3-7.

**Analysis** For an ideal gas at constant temperature  $T_0$ ,

$$PV = mRT_0 = C \quad \text{or} \quad P = \frac{C}{V}$$

where  $C$  is a constant. Substituting this into Eq. 3-11, we have

$$W_b = \int_1^2 P dV = \int_1^2 \frac{C}{V} dV = C \int_1^2 \frac{dV}{V} = C \ln \frac{V_2}{V_1} = P_1 V_1 \ln \frac{V_2}{V_1} \quad (3-16)$$

In the above equation,  $P_1 V_1$  can be replaced by  $P_2 V_2$  or  $mRT_0$ . Also,  $V_2/V_1$  can be replaced by  $P_1/P_2$  for this case since  $P_1 V_1 = P_2 V_2$ .

Substituting the numerical values into the above equation yields

$$\begin{aligned} W_b &= (100 \text{ kPa})(0.4 \text{ m}^3) \left( \ln \frac{0.1}{0.4} \right) \left( \frac{1 \text{ kJ}}{1 \text{ kPa} \cdot \text{m}^3} \right) \\ &= -55.45 \text{ kJ} \end{aligned}$$

# Polytropic Process

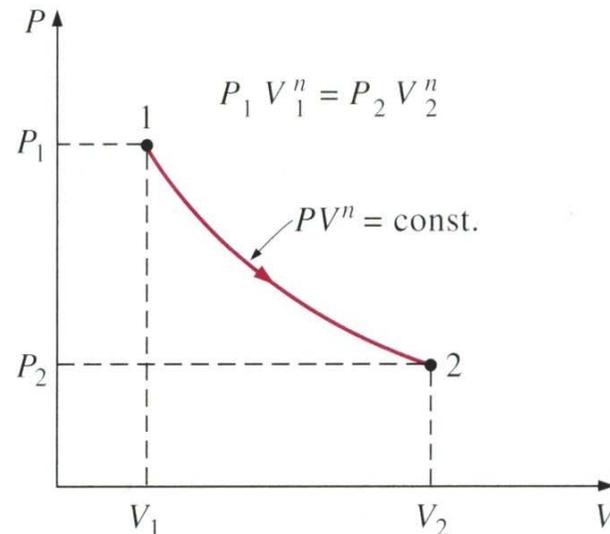
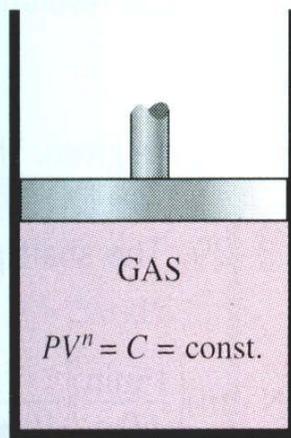
$$PV^n = C$$

sure for a polytropic process can be expressed as

$$P = CV^{-n} \quad (3-17)$$

Substituting this relation into Eq. 3-11, we obtain

$$W_b = \int_1^2 P dV = \int_1^2 CV^{-n} dV = C \frac{V_2^{-n+1} - V_1^{-n+1}}{-n+1} = \frac{P_2 V_2 - P_1 V_1}{1-n} \quad (3-18)$$



**FIGURE 3-26**

Schematic and  $P$ - $V$  diagram for a polytropic process.

---

since  $C = P_1V_1^n = P_2V_2^n$ . For an ideal gas ( $PV = mRT$ ), this equation can be written as

$$W_b = \frac{mR(T_2 - T_1)}{1 - n} \quad n \neq 1 \quad (\text{kJ}) \quad (3)$$

For the special case of  $n = 1$  the boundary work becomes

$$W_b = \int_1^2 P dV = \int_1^2 CV^{-1} dV = PV \ln \left( \frac{V_2}{V_1} \right)$$

For an ideal gas this result is equivalent to the isothermal process discussed in the previous example.

## 2 Shaft Work

Energy transmission with a rotating shaft is very common in engineering practice (Fig. 3–27). Often the torque  $\mathbf{T}$  applied to the shaft is constant, which means that the force  $F$  applied is also constant. For a specified constant torque, the work done during  $n$  revolutions is determined as follows: A force  $F$  acting through a moment arm  $r$  generates a torque  $\mathbf{T}$  of

$$\mathbf{T} = Fr \longrightarrow F = \frac{\mathbf{T}}{r}$$

This force acts through a distance  $s$ , which is related to the

$$s = (2\pi r)n$$

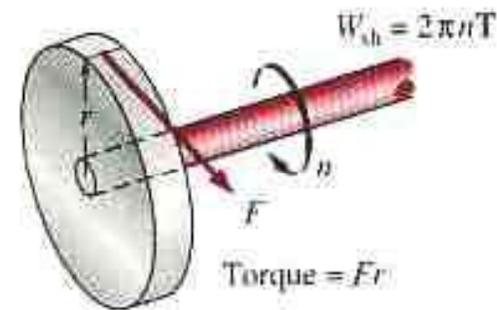
Then the shaft work is determined from

$$W_{\text{sh}} = Fs = \left(\frac{T}{r}\right)(2\pi rn) = 2\pi nT \quad (\text{kJ})$$

The power transmitted through the shaft is the shaft work done per unit time, which can be expressed as

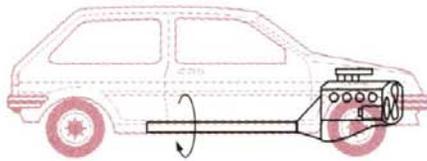
$$\dot{W}_{\text{sh}} = 2\pi \dot{n}T \quad (\text{kW}) \quad (3-1)$$

where  $\dot{n}$  is the number of revolutions per unit time.



**FIGURE 3–28**

Shaft work is proportional to the torque applied and the number of revolutions of the shaft.



$$n = 4000 \text{ rpm}$$
$$\tau = 200 \text{ Nm}$$

**FIGURE 3–29**

Schematic for Example 3–8.

### **EXAMPLE 3–8** Power Transmission by the Shaft of a Car

Determine the power transmitted through the shaft of a car when the torque applied is  $200 \text{ N} \cdot \text{m}$  and the shaft rotates at a rate of 4000 revolutions per minute (rpm).

**SOLUTION** The torque and the rpm for a car engine are given. The power transmitted is to be determined.

**Analysis** A sketch of the car is given in Fig. 3–29. The shaft power is determined directly from

$$\begin{aligned}\dot{W}_{\text{sh}} &= 2\pi n \mathbf{T} = (2\pi) \left( 4000 \frac{1}{\text{min}} \right) (200 \text{ N} \cdot \text{m}) \left( \frac{1 \text{ min}}{60 \text{ s}} \right) \left( \frac{1 \text{ kJ}}{1000 \text{ N} \cdot \text{m}} \right) \\ &= \mathbf{83.8 \text{ kW}} \text{ (or } 112.3 \text{ hp)}\end{aligned}$$

## Spring Work

It is common knowledge that when a force is applied on a spring, the length of the spring changes (Fig. 3–30). When the length of the spring changes by a differential amount  $dx$  under the influence of a force  $F$ , the work done is

$$\delta W_{\text{spring}} = F dx \quad (3-24)$$

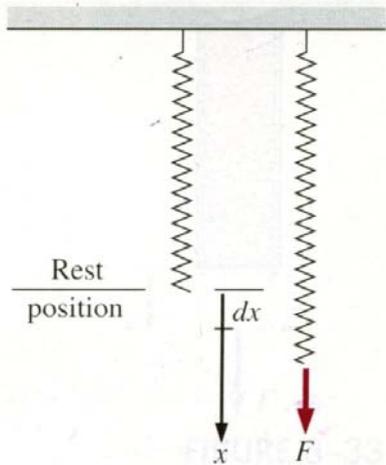
To determine the total spring work, we need to know a functional relationship between  $F$  and  $x$ . For linear elastic springs, the displacement  $x$  is proportional to the force applied (Fig. 3–31). That is,

$$F = kx \quad (\text{kN}) \quad (3-25)$$

where  $k$  is the spring constant and has the unit kN/m. The displacement  $x$  is measured from the undisturbed position of the spring (that is,  $x = 0$  when  $F = 0$ ). Substituting Eq. 3–25 into Eq. 3–24 and integrating yields

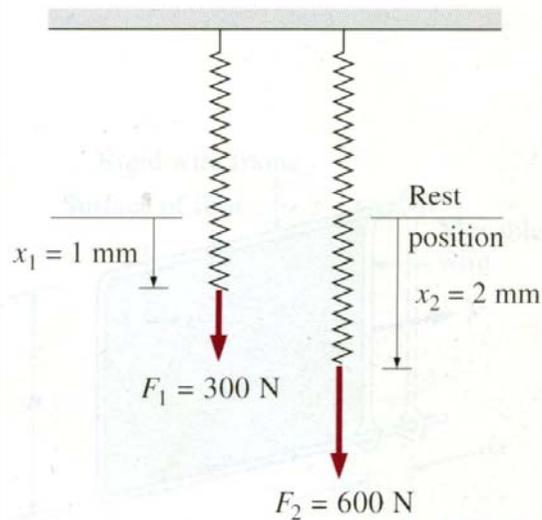
$$W_{\text{spring}} = \frac{1}{2}k(x_2^2 - x_1^2) \quad (\text{kJ}) \quad (3-26)$$

where  $x_1$  and  $x_2$  are the initial and the final displacements of the spring, respectively, measured from the undisturbed position of the spring.



**FIGURE 3-30**

Elongation of a spring under the influence of a force.



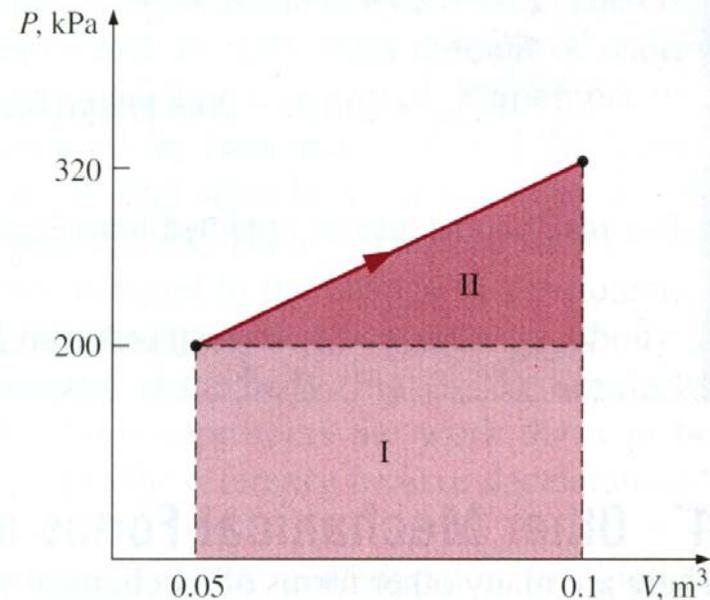
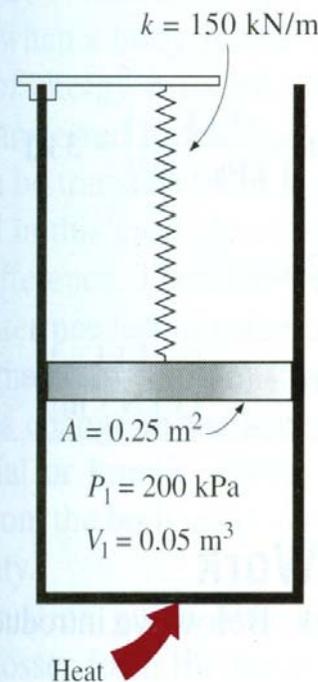
**FIGURE 3-31**

The displacement of a linear spring doubles when the force is doubled.

### EXAMPLE 3-9 Expansion of a Gas against a Spring

A piston-cylinder device contains  $0.05\text{ m}^3$  of a gas initially at  $200\text{ kPa}$ . At this state, a linear spring that has a spring constant of  $150\text{ kN/m}$  is touching the piston but exerting no force on it. Now heat is transferred to the gas, causing the piston to rise and to compress the spring until the volume inside the cylinder doubles. If the cross-sectional area of the piston is  $0.25\text{ m}^2$ , determine (a) the final pressure inside the cylinder, (b) the total work done by the gas, and (c) the fraction of this work done against the spring to compress it.

**SOLUTION** A sketch of the system and the  $P$ - $V$  diagram of the process are shown in Fig. 3-32.



**Assumptions** 1 The expansion process is quasi-equilibrium. 2 The spring is linear in the range of interest.

**Analysis** (a) The enclosed volume at the final state is

$$V_2 = 2V_1 = (2)(0.05 \text{ m}^3) = 0.1 \text{ m}^3$$

Then the displacement of the piston (and of the spring) becomes

$$x = \frac{\Delta V}{A} = \frac{(0.1 - 0.05) \text{ m}^3}{0.25 \text{ m}^2} = 0.2 \text{ m}$$

The force applied by the linear spring at the final state is

$$F = kx = (150 \text{ kN/m})(0.2 \text{ m}) = 30 \text{ kN}$$

The additional pressure applied by the spring on the gas at this state is

$$P = \frac{F}{A} = \frac{30 \text{ kN}}{0.25 \text{ m}^2} = 120 \text{ kPa}$$

Without the spring, the pressure of the gas would remain constant at 200 kPa while the piston is rising. But under the effect of the spring, the pressure rises linearly from 200 kPa to

$$200 + 120 = 320 \text{ kPa}$$

at the final state.

(b) An easy way of finding the work done is to plot the process on a  $P$ - $V$  diagram and find the area under the process curve. From Fig. 3-32 the area under the process curve (a trapezoid) is determined to be

$$W = \text{area} = \frac{(200 + 320) \text{ kPa}}{2} [(0.1 - 0.05) \text{ m}^3] \left( \frac{1 \text{ kJ}}{1 \text{ kPa} \cdot \text{m}^3} \right) = 13 \text{ kJ}$$

Note that the work is done by the system.

(c) The work represented by the rectangular area (region I) is done against the piston and the atmosphere, and the work represented by the triangular area (region II) is done against the spring. Thus,

$$W_{\text{spring}} = \frac{1}{2}[(320 - 200) \text{ kPa}](0.05 \text{ m}^3) \left( \frac{1 \text{ kJ}}{1 \text{ kPa} \cdot \text{m}^3} \right) = 3 \text{ kJ}$$

This result could also be obtained from Eq. 3-26:

$$W_{\text{spring}} = \frac{1}{2}k(x_2^2 - x_1^2) = \frac{1}{2}(150 \text{ kN/m})[(0.2 \text{ m})^2 - 0^2] \left( \frac{1 \text{ kJ}}{1 \text{ kN} \cdot \text{m}} \right) = 3 \text{ kJ}$$